

Auto1 - Logique et numération

—

Exercices supplémentaires

Brice COLOMBIER

2024

Tables de vérité et équations non simplifiées

Donner l'équation non simplifiée de la sortie s

a	b	c	s
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0

$s =$

a	b	c	s
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

$s =$

a	b	c	s
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

$s =$

a	b	c	d	s
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	1
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$s =$

Tables de vérité et équations non simplifiées (correction)

Donner l'équation non simplifiée de la sortie s

a	b	c	s
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0

$$s = a \cdot \bar{b} \cdot \bar{c} \vee b \cdot \bar{a} \cdot \bar{c}$$

a	b	c	s
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

$$s = a \cdot b \cdot c \vee a \cdot \bar{b} \cdot \bar{c}$$

a	b	c	s
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

$$s = a \cdot b \cdot \bar{c} \vee a \cdot c \cdot \bar{b} \vee \bar{a} \cdot \bar{b} \cdot \bar{c}$$

a	b	c	d	s
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$$s = a \cdot b \cdot \bar{c} \cdot \bar{d} \vee a \cdot c \cdot \bar{b} \cdot \bar{d} \vee b \cdot c \cdot d \cdot \bar{a} \vee d \cdot \bar{a} \cdot \bar{b} \cdot \bar{c} \vee \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d}$$

a	b	c	d	s
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

$$s = a \cdot b \cdot c \cdot \bar{d} \vee a \cdot b \cdot d \cdot \bar{c} \vee a \cdot c \cdot d \cdot \bar{b} \vee b \cdot d \cdot \bar{a} \cdot \bar{c} \vee c \cdot d \cdot \bar{a} \cdot \bar{b} \vee \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d}$$

a	b	c	d	s
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$$s = a \cdot b \cdot d \cdot \bar{c} \vee a \cdot b \cdot \bar{c} \cdot \bar{d} \vee a \cdot d \cdot \bar{b} \cdot \bar{c} \vee a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} \vee b \cdot c \cdot d \cdot \bar{a} \vee c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d} \vee \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d}$$

a	b	c	d	s
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$$s = a \cdot c \cdot d \cdot \bar{b} \vee a \cdot c \cdot \bar{b} \cdot \bar{d} \vee a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} \vee b \cdot c \cdot \bar{a} \cdot \bar{d} \vee c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d}$$

a	b	c	d	s
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$$s = a \cdot b \cdot \bar{c} \cdot \bar{d} \vee a \cdot c \cdot d \cdot \bar{b} \vee a \cdot c \cdot \bar{b} \cdot \bar{d} \vee a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} \vee b \cdot c \cdot d \cdot \bar{a} \vee b \cdot d \cdot \bar{a} \cdot \bar{c} \vee b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} \vee c \cdot d \cdot \bar{a} \cdot \bar{b}$$

a	b	c	d	s
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	1
1	1	1	1	0

$$s = a \cdot b \cdot c \cdot \bar{d} \vee a \cdot b \cdot \bar{c} \cdot \bar{d} \vee a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} \vee b \cdot c \cdot d \cdot \bar{a} \vee b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} \vee d \cdot \bar{a} \cdot \bar{b} \cdot \bar{c} \vee \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d}$$

a	b	c	d	s
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$$s = a \cdot b \cdot d \cdot \bar{c} \vee a \cdot c \cdot \bar{b} \cdot \bar{d} \vee a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} \vee b \cdot d \cdot \bar{a} \cdot \bar{c} \vee b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} \vee d \cdot \bar{a} \cdot \bar{b} \cdot \bar{c}$$

Simplification d'équations

Simplifier ces équations avec les règles de l'algèbre de Boole.

$$a \cdot b + b \cdot \bar{a} =$$

$$a \cdot b + a \cdot \bar{b} + \bar{a} \cdot \bar{b} =$$

$$a \cdot b + a \cdot \bar{b} =$$

$$a \cdot \bar{b} + b \cdot \bar{a} + \bar{a} \cdot \bar{b} =$$

$$a \cdot b \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} =$$

$$a \cdot b \cdot c + a \cdot c \cdot \bar{b} + a \cdot \bar{b} \cdot \bar{c} + b \cdot c \cdot \bar{a} =$$

$$b \cdot \bar{a} + b \cdot \bar{c} + a \cdot b \cdot c =$$

$$\bar{a} \cdot \bar{c} + \bar{b} \cdot \bar{c} + a \cdot b \cdot \bar{c} =$$

$$a \cdot b + a \cdot b \cdot c + a \cdot c \cdot \bar{b} + a \cdot \bar{b} \cdot \bar{c} + c \cdot \bar{a} \cdot \bar{b} =$$

$$b \cdot c + c \cdot \bar{b} + \bar{a} \cdot \bar{b} \cdot \bar{c} =$$

$$b \cdot \bar{c} + a \cdot b \cdot c + a \cdot b \cdot \bar{c} + a \cdot c \cdot \bar{b} + b \cdot \bar{a} \cdot \bar{c} =$$

$$a \cdot b \cdot c + a \cdot c \cdot \bar{b} + a \cdot \bar{b} \cdot \bar{c} =$$

$$c \cdot \bar{a} + a \cdot b \cdot c + a \cdot c \cdot \bar{b} + b \cdot c \cdot \bar{a} + c \cdot \bar{a} \cdot \bar{b} =$$

$$a \cdot b \cdot c + b \cdot c \cdot \bar{a} + b \cdot \bar{a} \cdot \bar{c} =$$

$$\bar{b} \cdot \bar{c} + a \cdot b \cdot \bar{c} + a \cdot c \cdot \bar{b} + c \cdot \bar{a} \cdot \bar{b} =$$

$$a \cdot b \cdot c + a \cdot c \cdot \bar{b} + b \cdot c \cdot \bar{a} + b \cdot \bar{a} \cdot \bar{c} + c \cdot \bar{a} \cdot \bar{b} =$$

$$b \cdot d \cdot \bar{c} + a \cdot c \cdot d \cdot \bar{b} + a \cdot c \cdot \bar{b} \cdot \bar{d} + a \cdot d \cdot \bar{b} \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} + d \cdot \bar{a} \cdot \bar{b} \cdot \bar{c} =$$

$$a \cdot b \cdot d + b \cdot c \cdot d + c \cdot d \cdot \bar{b} + a \cdot b \cdot \bar{c} \cdot \bar{d} =$$

$$c \cdot \bar{b} \cdot \bar{d} + a \cdot c \cdot d \cdot \bar{b} + a \cdot c \cdot \bar{b} \cdot \bar{d} + b \cdot d \cdot \bar{a} \cdot \bar{c} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} + c \cdot d \cdot \bar{a} \cdot \bar{b} + c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d} =$$

$$a \cdot b \cdot d + a \cdot d \cdot \bar{c} + a \cdot c \cdot d \cdot \bar{b} + b \cdot c \cdot d \cdot \bar{a} + b \cdot d \cdot \bar{a} \cdot \bar{c} =$$

$$a \cdot b \cdot d + a \cdot b \cdot \bar{c} + b \cdot c \cdot d + a \cdot b \cdot c \cdot \bar{d} + a \cdot b \cdot \bar{c} \cdot \bar{d} + b \cdot c \cdot d \cdot \bar{a} =$$

$$a \cdot b \cdot d + a \cdot c \cdot \bar{d} + a \cdot \bar{b} \cdot \bar{d} + a \cdot b \cdot c \cdot d + a \cdot b \cdot \bar{c} \cdot \bar{d} =$$

$$a \cdot c \cdot d + b \cdot d \cdot \bar{a} + b \cdot d \cdot \bar{c} + c \cdot d \cdot \bar{b} + d \cdot \bar{a} \cdot \bar{b} + a \cdot b \cdot c \cdot d + a \cdot d \cdot \bar{b} \cdot \bar{c} + b \cdot c \cdot d \cdot \bar{a} + c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d} =$$

$$a \cdot b \cdot d + a \cdot \bar{b} \cdot \bar{d} + a \cdot b \cdot c \cdot \bar{d} + a \cdot b \cdot \bar{c} \cdot \bar{d} + a \cdot c \cdot d \cdot \bar{b} + a \cdot d \cdot \bar{b} \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} + b \cdot c \cdot d \cdot \bar{a} + b \cdot c \cdot \bar{a} \cdot \bar{d} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} + c \cdot d \cdot \bar{a} \cdot \bar{b} =$$

$$b \cdot \bar{a} \cdot \bar{d} + c \cdot d \cdot \bar{a} + c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d} + \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} =$$

$$a \cdot b \cdot d + a \cdot b \cdot \bar{c} + b \cdot d \cdot \bar{a} \cdot \bar{c} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} =$$

$$a \cdot \bar{b} \cdot \bar{c} + b \cdot c \cdot \bar{a} + b \cdot c \cdot \bar{d} + d \cdot \bar{b} \cdot \bar{c} + \bar{b} \cdot \bar{c} \cdot \bar{d} + a \cdot b \cdot c \cdot d + a \cdot d \cdot \bar{b} \cdot \bar{c} =$$

$$a \cdot d \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} + a \cdot b \cdot d \cdot \bar{c} + a \cdot b \cdot \bar{c} \cdot \bar{d} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} + \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} =$$

Simplification d'équations (correction)

Simplifier ces équations avec les règles de l'algèbre de Boole.

$$a \cdot b + b \cdot \bar{a} = b$$

$$a \cdot b + a \cdot \bar{b} + \bar{a} \cdot \bar{b} = a + \bar{b}$$

$$a \cdot b + a \cdot \bar{b} = a$$

$$a \cdot \bar{b} + b \cdot \bar{a} + \bar{a} \cdot \bar{b} = \bar{a} + \bar{b}$$

$$a \cdot b \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} = a \cdot \bar{c}$$

$$a \cdot b \cdot c + a \cdot c \cdot \bar{b} + a \cdot \bar{b} \cdot \bar{c} + b \cdot c \cdot \bar{a} = a \cdot \bar{b} + b \cdot c$$

$$b \cdot \bar{a} + b \cdot \bar{c} + a \cdot b \cdot c = b$$

$$\bar{a} \cdot \bar{c} + \bar{b} \cdot \bar{c} + a \cdot b \cdot \bar{c} = \bar{c}$$

$$a \cdot b + a \cdot b \cdot c + a \cdot c \cdot \bar{b} + a \cdot \bar{b} \cdot \bar{c} + c \cdot \bar{a} \cdot \bar{b} = a + c \cdot \bar{b}$$

$$b \cdot c + c \cdot \bar{b} + \bar{a} \cdot \bar{b} \cdot \bar{c} = c + \bar{a} \cdot \bar{b}$$

$$b \cdot \bar{c} + a \cdot b \cdot c + a \cdot b \cdot \bar{c} + a \cdot c \cdot \bar{b} + b \cdot \bar{a} \cdot \bar{c} = a \cdot c + b \cdot \bar{c}$$

$$a \cdot b \cdot c + a \cdot c \cdot \bar{b} + a \cdot \bar{b} \cdot \bar{c} = a \cdot c + a \cdot \bar{b}$$

$$c \cdot \bar{a} + a \cdot b \cdot c + a \cdot c \cdot \bar{b} + b \cdot c \cdot \bar{a} + c \cdot \bar{a} \cdot \bar{b} = c$$

$$a \cdot b \cdot c + b \cdot c \cdot \bar{a} + b \cdot \bar{a} \cdot \bar{c} = b \cdot c + b \cdot \bar{a}$$

$$\bar{b} \cdot \bar{c} + a \cdot b \cdot \bar{c} + a \cdot c \cdot \bar{b} + c \cdot \bar{a} \cdot \bar{b} = a \cdot \bar{c} + \bar{b}$$

$$a \cdot b \cdot c + a \cdot c \cdot \bar{b} + b \cdot c \cdot \bar{a} + b \cdot \bar{a} \cdot \bar{c} + c \cdot \bar{a} \cdot \bar{b} = c + b \cdot \bar{a}$$

$$b \cdot d \cdot \bar{c} + a \cdot c \cdot d \cdot \bar{b} + a \cdot c \cdot \bar{b} \cdot \bar{d} + a \cdot d \cdot \bar{b} \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} + d \cdot \bar{a} \cdot \bar{b} \cdot \bar{c} = a \cdot \bar{b} + d \cdot \bar{c}$$

$$a \cdot b \cdot d + b \cdot c \cdot d + c \cdot d \cdot \bar{b} + a \cdot b \cdot \bar{c} \cdot \bar{d} = c \cdot d + a \cdot b \cdot \bar{c}$$

$$c \cdot \bar{b} \cdot \bar{d} + a \cdot c \cdot d \cdot \bar{b} + a \cdot c \cdot \bar{b} \cdot \bar{d} + b \cdot d \cdot \bar{a} \cdot \bar{c} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} + c \cdot d \cdot \bar{a} \cdot \bar{b} + c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d} = c \cdot \bar{b} + b \cdot \bar{a} \cdot \bar{c}$$

$$a \cdot b \cdot d + a \cdot d \cdot \bar{c} + a \cdot c \cdot d \cdot \bar{b} + b \cdot c \cdot d \cdot \bar{a} + b \cdot d \cdot \bar{a} \cdot \bar{c} = a \cdot d + b \cdot d$$

$$a \cdot b \cdot d + a \cdot b \cdot \bar{c} + b \cdot c \cdot d + a \cdot b \cdot c \cdot \bar{d} + a \cdot b \cdot \bar{c} \cdot \bar{d} + b \cdot c \cdot d \cdot \bar{a} = a \cdot b + b \cdot c \cdot d$$

$$a \cdot b \cdot d + a \cdot c \cdot \bar{d} + a \cdot \bar{b} \cdot \bar{d} + a \cdot b \cdot c \cdot d + a \cdot b \cdot \bar{c} \cdot \bar{d} = a \cdot b + a \cdot \bar{d}$$

$$a \cdot c \cdot d + b \cdot d \cdot \bar{a} + b \cdot d \cdot \bar{c} + c \cdot d \cdot \bar{b} + d \cdot \bar{a} \cdot \bar{b} + a \cdot b \cdot c \cdot d + a \cdot d \cdot \bar{b} \cdot \bar{c} + b \cdot c \cdot d \cdot \bar{a} + c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d} = d + c \cdot \bar{a} \cdot \bar{b}$$

$$a \cdot b \cdot d + a \cdot \bar{b} \cdot \bar{d} + a \cdot b \cdot c \cdot \bar{d} + a \cdot b \cdot \bar{c} \cdot \bar{d} + a \cdot c \cdot d \cdot \bar{b} + a \cdot d \cdot \bar{b} \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} + b \cdot c \cdot d \cdot \bar{a} + b \cdot c \cdot \bar{a} \cdot \bar{d} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} + c \cdot d \cdot \bar{a} \cdot \bar{b} = a + b \cdot \bar{d} + c \cdot d$$

$$b \cdot \bar{a} \cdot \bar{d} + c \cdot d \cdot \bar{a} + c \cdot \bar{a} \cdot \bar{b} \cdot \bar{d} + \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} = c \cdot \bar{a} + \bar{a} \cdot \bar{d}$$

$$a \cdot b \cdot d + a \cdot b \cdot \bar{c} + b \cdot d \cdot \bar{a} \cdot \bar{c} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} = b \cdot \bar{c} + a \cdot b \cdot d$$

$$a \cdot \bar{b} \cdot \bar{c} + b \cdot c \cdot \bar{a} + b \cdot c \cdot \bar{d} + d \cdot \bar{b} \cdot \bar{c} + \bar{b} \cdot \bar{c} \cdot \bar{d} + a \cdot b \cdot c \cdot d + a \cdot d \cdot \bar{b} \cdot \bar{c} = b \cdot c + \bar{b} \cdot \bar{c}$$

$$a \cdot d \cdot \bar{c} + a \cdot \bar{b} \cdot \bar{c} + a \cdot b \cdot d \cdot \bar{c} + a \cdot b \cdot \bar{c} \cdot \bar{d} + b \cdot \bar{a} \cdot \bar{c} \cdot \bar{d} + \bar{a} \cdot \bar{b} \cdot \bar{c} \cdot \bar{d} = a \cdot \bar{c} + \bar{c} \cdot \bar{d}$$

Tableaux de Karnaugh

À partir de la table de vérité, utiliser la méthode du tableau de Karnaugh pour obtenir l'équation logique simplifiée.

a	b	c	s
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

$s =$

a	b	c	s
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0

$s =$

a	b	c	s
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

$s =$

a	b	c	d	s
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

$s =$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$s =$

Tableaux de Karnaugh (correction)

À partir de la table de vérité, utiliser la méthode du tableau de Karnaugh pour obtenir l'équation logique simplifiée.

a	b	c	s
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

$$s = a \cdot c + b \cdot \bar{a}$$

a	b	c	s
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0

$$s = b \cdot \bar{a} + \bar{b} \cdot \bar{c}$$

a	b	c	s
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

$$s = b \cdot c + \bar{a} \cdot \bar{c}$$

a	b	c	d	s
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	0

$$s = c \cdot \bar{a} + c \cdot \bar{d} + a \cdot b \cdot \bar{c}$$

a	b	c	d	s
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$$s = a \cdot \bar{b} + c \cdot \bar{b} + c \cdot d \cdot \bar{a}$$

a	b	c	d	s
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

$$s = b \cdot c + c \cdot \bar{d} + \bar{a} \cdot \bar{d}$$

a	b	c	d	s
0	0	0	0	1
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

$$s = b \cdot c + \bar{b} \cdot \bar{c}$$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$$s = a \cdot b + a \cdot c + b \cdot d \cdot \bar{c}$$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

$$s = b \cdot d + d \cdot \bar{a} + d \cdot \bar{c}$$

<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>s</i>
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	0

$$s = a \cdot \bar{b} + a \cdot \bar{c} + c \cdot d \cdot \bar{b}$$

Conversions

Compléter les cases vides du tableau en convertissant entre les bases.

Binaire	Décimal	Hexadécimal
1101 ₍₂₎		
	7 ₍₁₀₎	
		2 ₍₁₆₎
110100 ₍₂₎		
	21 ₍₁₀₎	
		10 ₍₁₆₎
10001 ₍₂₎		
	9 ₍₁₀₎	
		12 ₍₁₆₎
0 ₍₂₎		
	37 ₍₁₀₎	
		BC ₍₁₆₎
1110001 ₍₂₎		
	378 ₍₁₀₎	
		A5 ₍₁₆₎
110001111 ₍₂₎		
	342 ₍₁₀₎	
		33 ₍₁₆₎
10101100 ₍₂₎		
	8628 ₍₁₀₎	
		1EF1 ₍₁₆₎
1000011111000 ₍₂₎		
	2289 ₍₁₀₎	
		1FE ₍₁₆₎
110100110010 ₍₂₎		
	3678 ₍₁₀₎	
		F51 ₍₁₆₎

Conversions (correction)

Compléter les cases vides du tableau en convertissant entre les bases.

Binaire	Décimal	Hexadécimal
1101 ₍₂₎	13 ₍₁₀₎	D ₍₁₆₎
111 ₍₂₎	7 ₍₁₀₎	7 ₍₁₆₎
10 ₍₂₎	2 ₍₁₀₎	2 ₍₁₆₎
110100 ₍₂₎	52 ₍₁₀₎	34 ₍₁₆₎
10101 ₍₂₎	21 ₍₁₀₎	15 ₍₁₆₎
10000 ₍₂₎	16 ₍₁₀₎	10 ₍₁₆₎
10001 ₍₂₎	17 ₍₁₀₎	11 ₍₁₆₎
1001 ₍₂₎	9 ₍₁₀₎	9 ₍₁₆₎
10010 ₍₂₎	18 ₍₁₀₎	12 ₍₁₆₎
0 ₍₂₎	0 ₍₁₀₎	0 ₍₁₆₎
100101 ₍₂₎	37 ₍₁₀₎	25 ₍₁₆₎
10111100 ₍₂₎	188 ₍₁₀₎	BC ₍₁₆₎
1110001 ₍₂₎	113 ₍₁₀₎	71 ₍₁₆₎
101111010 ₍₂₎	378 ₍₁₀₎	17A ₍₁₆₎
10100101 ₍₂₎	165 ₍₁₀₎	A5 ₍₁₆₎
110001111 ₍₂₎	399 ₍₁₀₎	18F ₍₁₆₎
101010110 ₍₂₎	342 ₍₁₀₎	156 ₍₁₆₎
110011 ₍₂₎	51 ₍₁₀₎	33 ₍₁₆₎
10101100 ₍₂₎	172 ₍₁₀₎	AC ₍₁₆₎
10000110110100 ₍₂₎	8628 ₍₁₀₎	21B4 ₍₁₆₎
1111011110001 ₍₂₎	7921 ₍₁₀₎	1EF1 ₍₁₆₎
1000011111000 ₍₂₎	4344 ₍₁₀₎	10F8 ₍₁₆₎
100011110001 ₍₂₎	2289 ₍₁₀₎	8F1 ₍₁₆₎
111111110 ₍₂₎	510 ₍₁₀₎	1FE ₍₁₆₎
110100110010 ₍₂₎	3378 ₍₁₀₎	D32 ₍₁₆₎
111001011110 ₍₂₎	3678 ₍₁₀₎	E5E ₍₁₆₎
111101010001 ₍₂₎	3921 ₍₁₀₎	F51 ₍₁₆₎

Nombres binaires signés

Compléter les cases vides du tableau en utilisant si nécessaire la méthode du complément à deux.

Binaire signé sur 8 bits	Décimal signé
01111011	
	-42
11111010	
	0
10010101	
	-112
10101111	
	31
00001010	
	-1
01110111	
	53
00110000	
	-31
11111100	
	-55
00000110	
	-128
01011110	
	127
11000001	
	106
10111001	
	45
11110101	
	36
00001100	
	97
11100000	
	-101

Nombres binaires signés (correction)

Compléter les cases vides du tableau en utilisant si nécessaire la méthode du complément à deux.

Binaire signé sur 8 bits	Décimal signé
01111011	123
11010110	-42
11111010	-6
00000000	0
10010101	-107
10010000	-112
10101111	-81
00011111	31
00001010	10
11111111	-1
01110111	119
00110101	53
00110000	48
11100001	-31
11111100	-4
11001001	-55
00000110	6
10000000	-128
01011110	94
01111111	127
11000001	-63
01101010	106
10111001	-71
00101101	45
11110101	-11
00100100	36
00001100	12
01100001	97
11100000	-32
10011011	-101